Exponents

Introduction

Whole number exponents stand for repeated multiplication.

For example, 4^3 or "four to the third power," means 4 times *itself* 3 times, or 4 x 4 x 4, or 4 · 4 · 4 The example, 4^3 , equals 64 because $4 \cdot 4 = 16$, which, multiplied by 4 a third time, equals 64.

In the example above, 4 is called the **base**, and 3 is called the **exponent**.



Another example:

 $8^4 = 8 \cdot 8 \cdot 8 \cdot 8$

 $8 \cdot 8 = 64$ $64 \cdot 8 = 512$ $512 \cdot 8 = 4096$ So, $8^4 = 4096$

In general, b^n is b times itself n times.

The term "squared" means raised to the second power. Three squared is 3^2 or $3 \cdot 3$ The term "cubed" means raised to the third power. Four cubed is 4^3 or $4 \cdot 4 \cdot 4$

Special Exponents

Any number to the power of 1 is the number you started with. For example:

 $9^1 = 9$ $4^1 = 4$ $1^1 = 1$ $1000^1 = 1,000$ $b^1 = b$

Any number to the 0 power is 1. For example:

 $9^0 = 1$ $4^0 = 1$ $1^0 = 1$ $1000^0 = 1$ $b^0 = 1$

Multiplying Exponential Expressions

When multiplying exponential expressions with the same base, keep the base the same and add the exponents. For example:

$$4^{3} \cdot 4^{5} = (4 \cdot 4 \cdot 4) \cdot (4 \cdot 4 \cdot 4 \cdot 4) = 4^{8} \qquad 7^{2} \cdot 7^{3} = (7 \cdot 7) \cdot (7 \cdot 7 \cdot 7) = 7^{5} \qquad b^{m} \cdot b^{n} = b^{m+n}$$

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$$\frac{5 \cdot 5 \cdot 5 \cdot 5}{5 \cdot 5} = 5^2 \qquad \frac{b^m}{b^n} = b^{m - n}$$